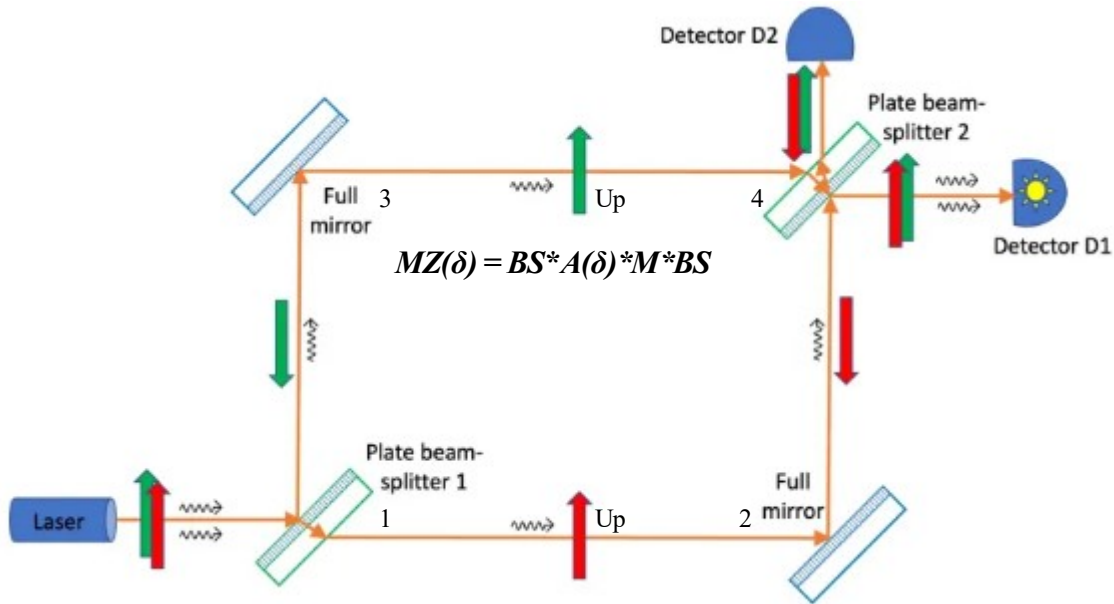


XVI. Quantitative Analysis of Phase Splitting on Mach-Zehnder Interferometer

Graphics: <https://quantumphysics-consciousness.eu/index.php/en/the-mach-zehnder-interferometer-explained/>

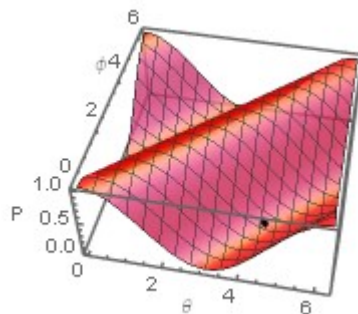
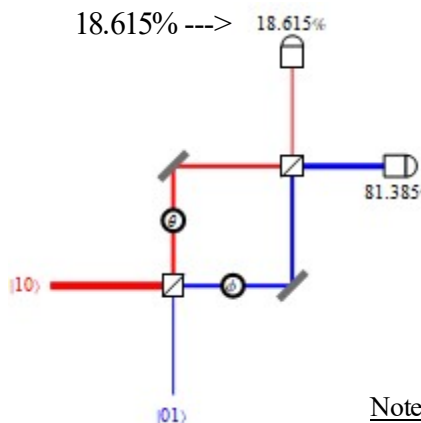
A wave can experience a phase shift (δ) upon full or partial reflection. This is a feature that is applied in the Mach-Zehnder interferometer, MZ, to induce phase differences in split light waves and thus invoke interference effects when they are combined again. Mach-Zehnder interferometer beam splitters (BS) are used to achieve several things:

- *split a light beam in two equal and synchronous beams, a reflected beam and a straight-through passing beam,
- *induce a phase (δ) shift in the reflected beam. NB: The straight-through passing beam does not experience phase shift.
- *recombine the two light beams in order to let them interfere.



Now we follow the waves that should reach detector D2. The Up wave traveling along 1-2-4 receives a 180° phase shift at beam splitter (BS) 1. Another 180° phase shift (δ) at full mirror 2. Then finally zero phase shift by the reflection from glass by Mirror (M) to air at beam splitter 4 in the direction of D2. Total is thus 360° . The wave D traveling along 1-3-4 receives only one phase shift at mirror 3 of 180° . So the recombined two waves going from beam splitter 4 to detector D2 will interfere with phase difference 180° , which means fully opposite phases. Which means destructive interference. D2 receives no light.

Mathematica: 3D Solution of Beam Probability with Relative Phase Shifts θ and ϕ .



Note P, θ , ϕ Location of above black dot.

Probability of going into top detector: P_{top}

$$P_{top}(\theta, \phi) := \cos\left(\frac{\theta - \phi}{2}\right)^2$$

$$P_{top}(2.24938, 0) = 18.615\%$$

beam splitter		$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$
mirror		$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
phase shifter		$\begin{pmatrix} e^{i\epsilon} & 0 \\ 0 & e^{i\phi} \end{pmatrix}$